



Sensing, Computing, Actuating

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ACOUSTIC SENSORS AND ACTUATORS

(Chapter 5.7)



bats
ultrasound (mechanical)



shark
electrical field



snake
thermal radiation



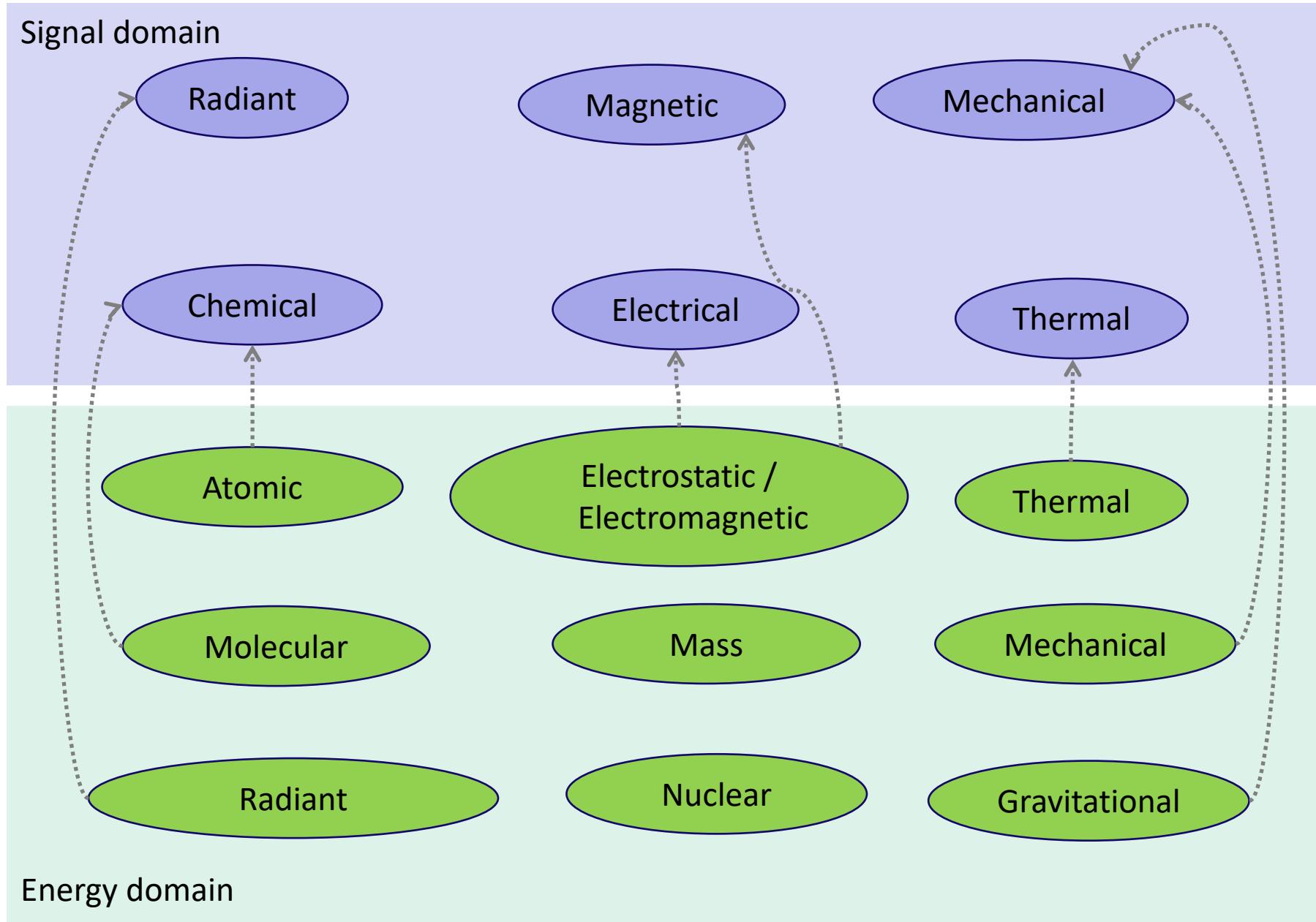
rats
touch (mechanical)

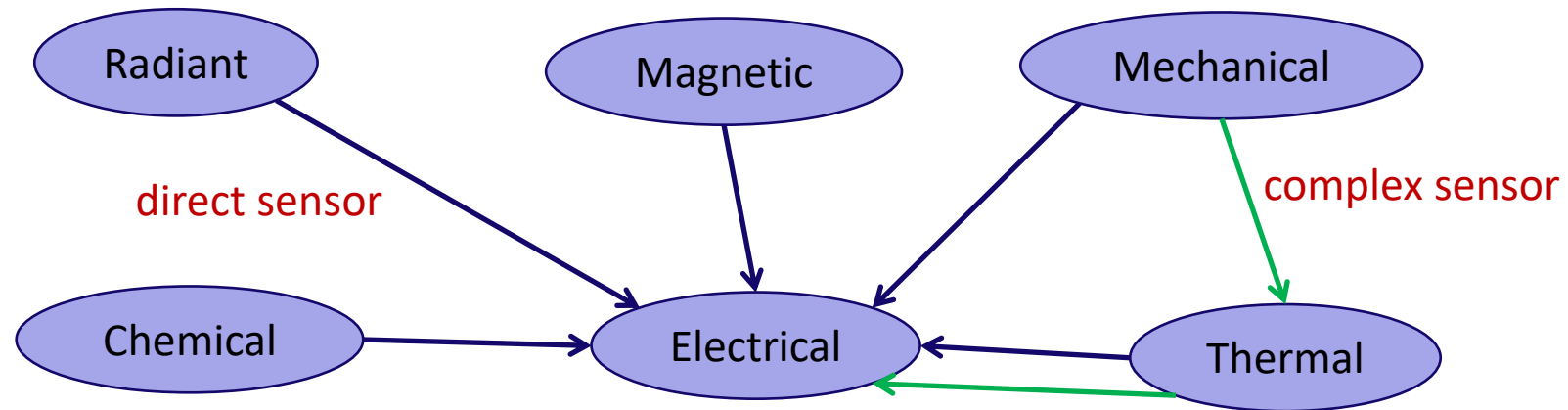


fish
sound vibrations
(mechanical)

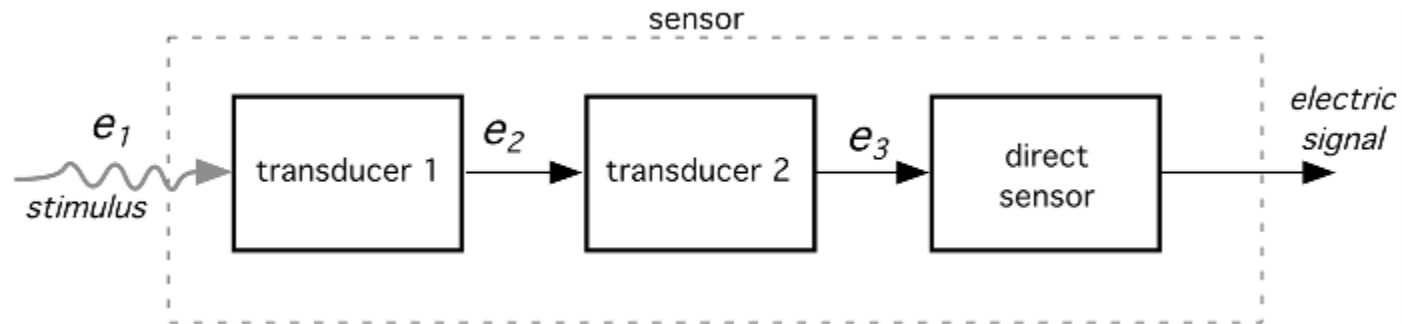


birds
magnetic field

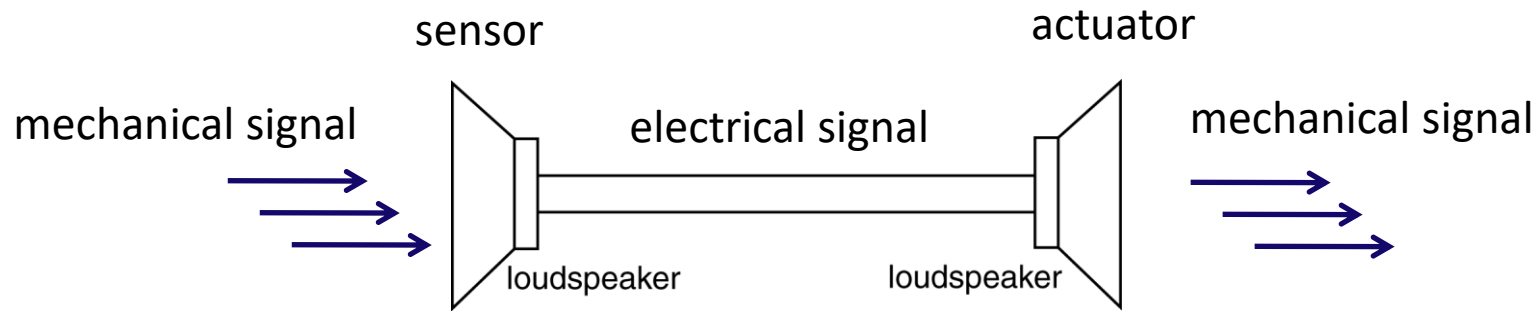




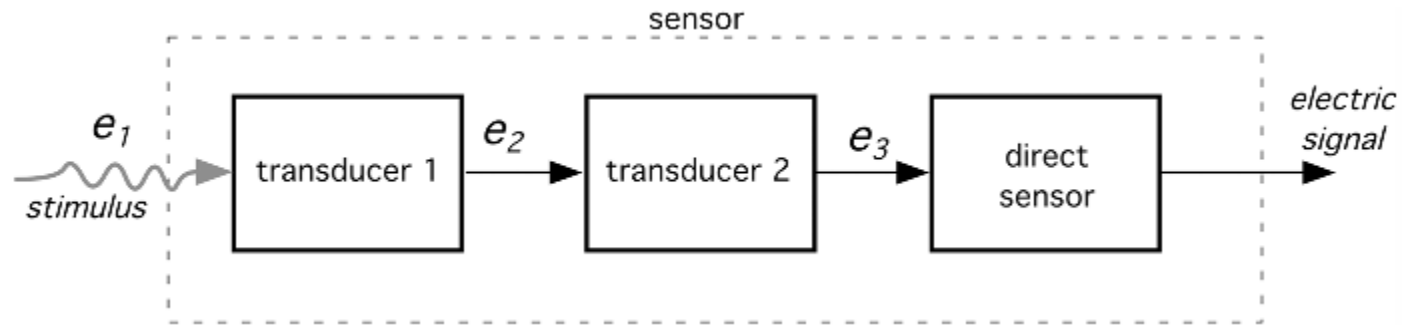
- a **transducer** converts a stimulus from a signal domain to another signal domain
- a **sensor** receives a stimulus and responds with an electrical signal



- an **actuator** converts an electrical signal to another signal domain



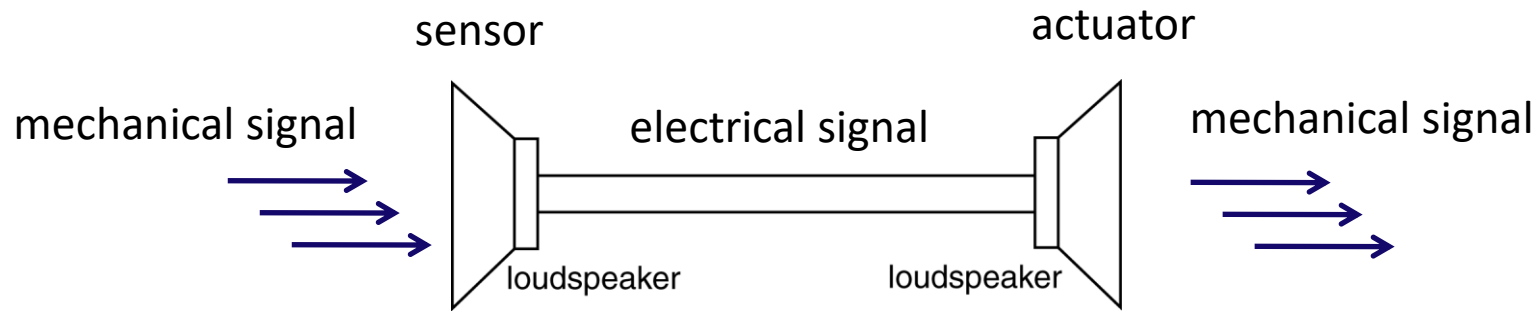
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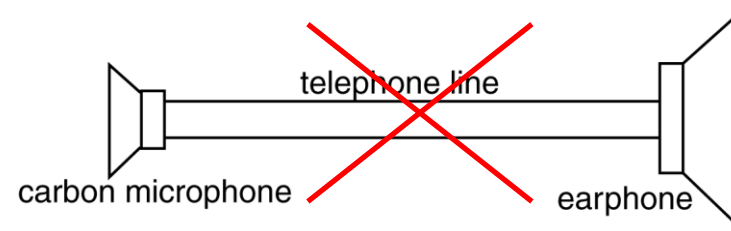
- an **actuator** converts an electrical signal to another signal domain

why do we prefer a transducer that produces a signal in the electrical domain?

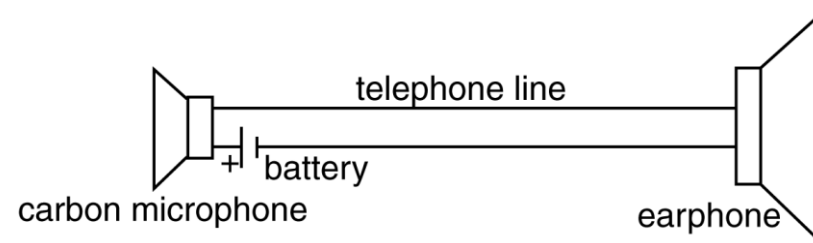
- a signal in **any domain** can be converted to a signal in the electrical domain
- energy does not have to be drained from the processes being measured, instead an **amplifier** can be used
- many **electrical signal conditioners** exist
- many options exist to **process**, **display** and **store** electrical information
- it is easy to **communicate** electrical signals

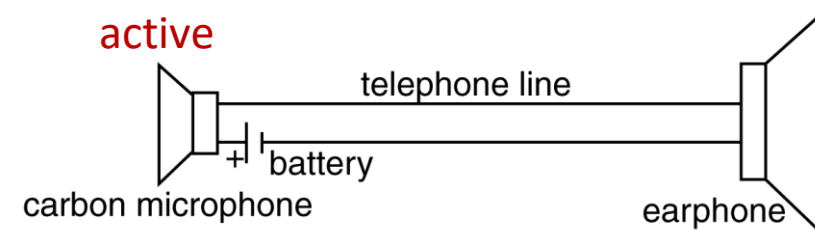
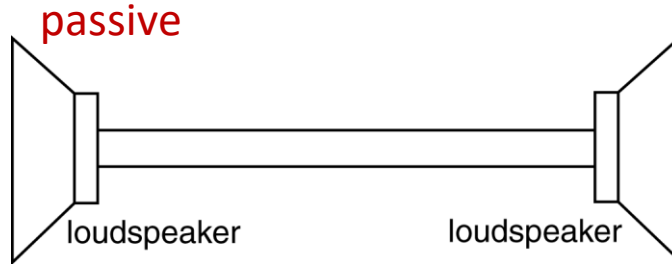


- a telephone works in a different way

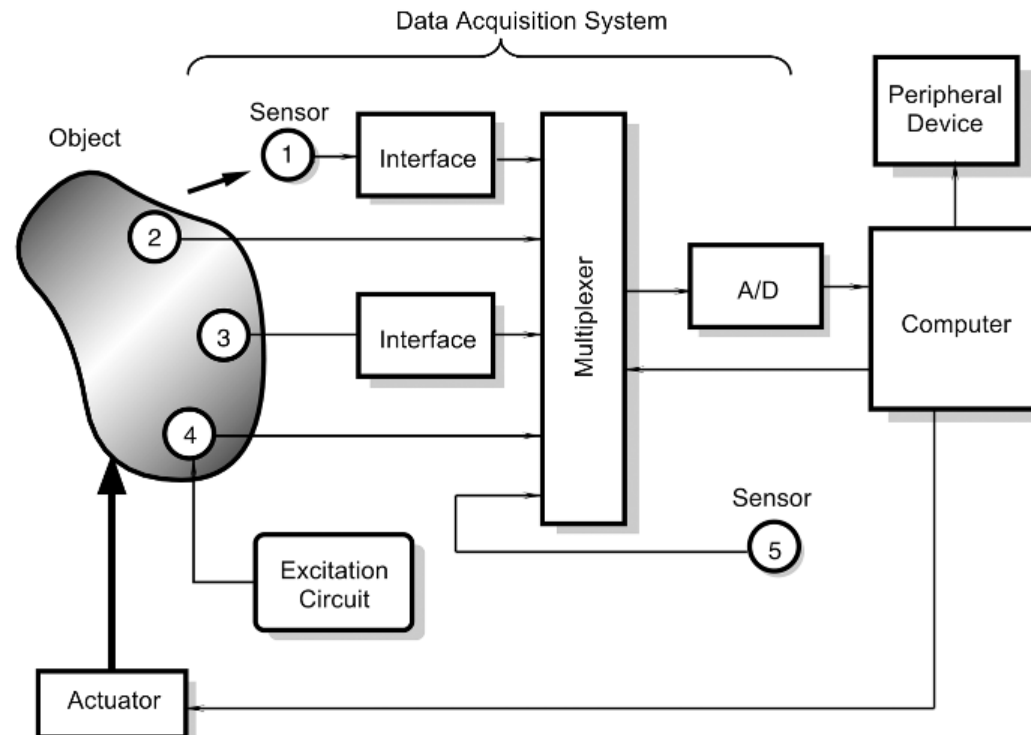


- microphone converts sound to change of resistance
- no transduction takes place (no change of energy)
- power source must be added to affect transduction





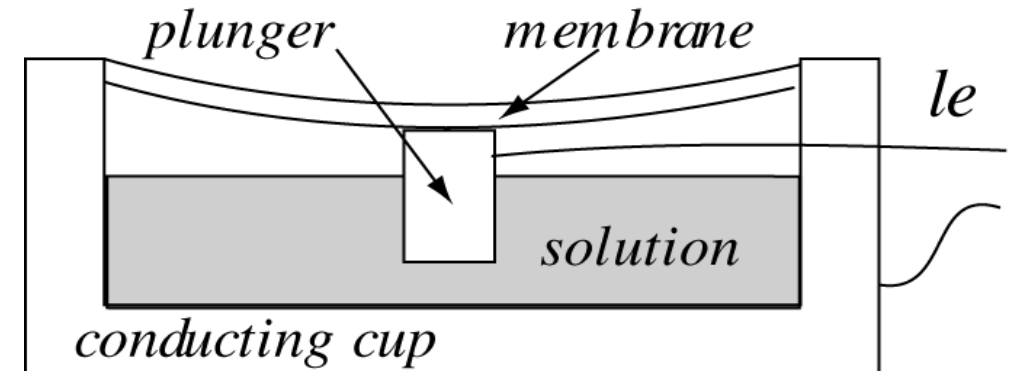
- an **active** sensor requires external power to operate
- a **passive** (**self-generating**) sensor generates its own electrical signal



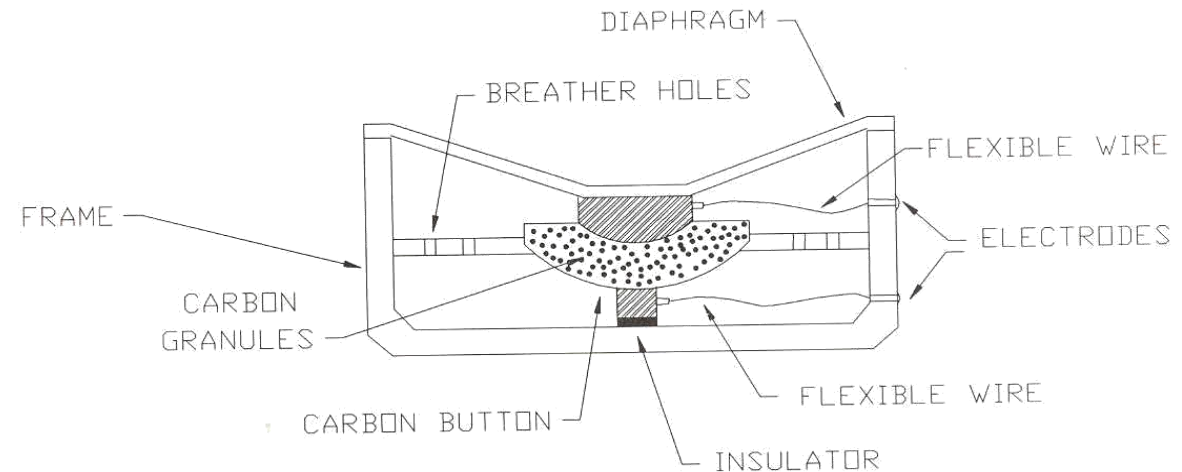
sensor classification

1	passive
2	passive
3	passive
4	active
5	passive

- microphones are sound sensors sensing change in pressure
- speakers are sound actuators
- first microphones and speakers were devised and patented for use in telephones
- Alexander Graham Bell patented the first variable resistance microphone in 1876
- operation
 - Pressure pushes membrane and plunger down in solution
 - Resistance between plunger and body of the microphone (cup) changes

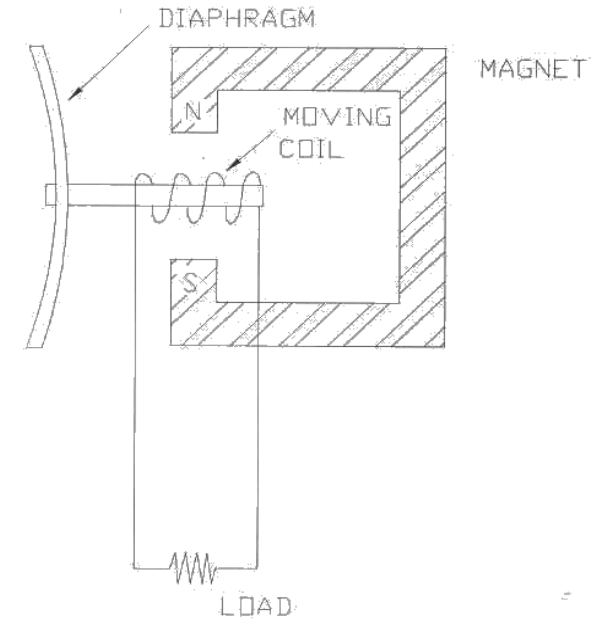


- first practical microphone invented by Thomas Edison in 1878
- solution in Bell's microphone is replaced with carbon or graphite particles
- bulk resistivity of the powder is sensitive to pressure
- variable resistive microphones have poor performance
 - limited dynamic range
 - poor frequency response
 - high noise floor

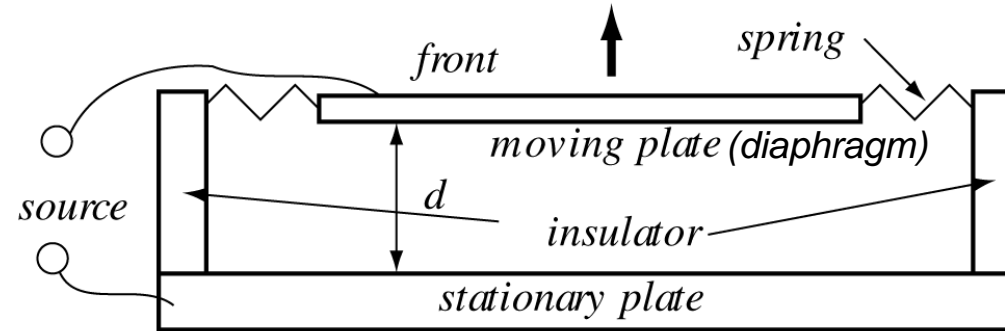


Moving coil microphone

- first microphone to produce the whole range of the human voice
- still in use today, although simpler devices have been developed
- device is fundamentally the same as a common loudspeaker
 - any small loudspeaker can serve as dynamic microphone
 - moving coil microphone is dual device capable of serving as loudspeaker or microphone (sensor and actuator)
- moving coil microphone offers
 - large dynamic range
 - good frequency response
 - relatively low noise level
 - high sensitivity



- Operation
 - allow sound to move a plate in a capacitor
 - sense the change in capacitance

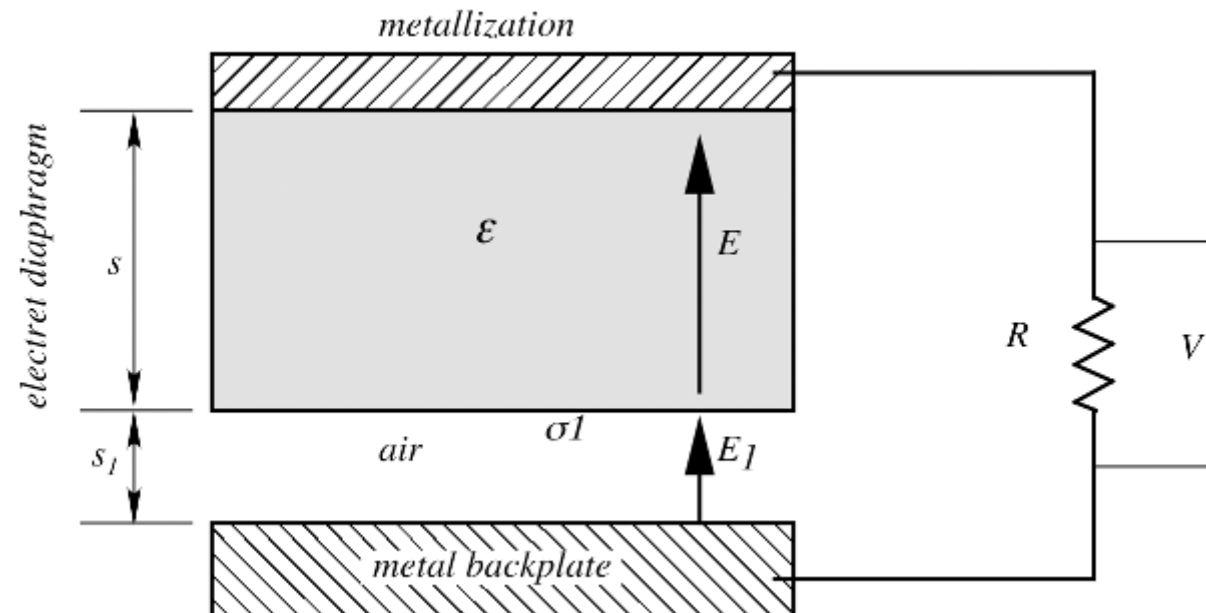


- operation based on basic equations for plate capacitor

$$C = \frac{\epsilon_0 \epsilon_r A}{d} \quad C = \frac{Q}{V} \quad \longrightarrow \quad V = Q \frac{d}{\epsilon_0 \epsilon_r A}$$

- output voltage proportional to distance between plates
- magnitude of electric charge source Q determines sensitivity

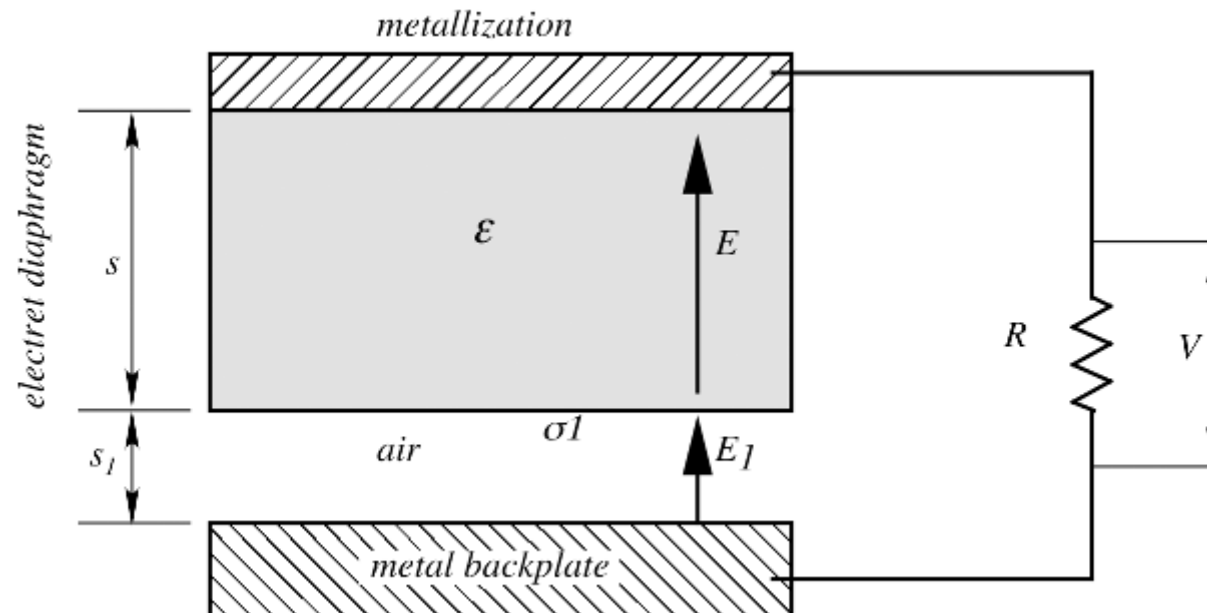
- electret microphone is a capacitive microphone used in many devices (e.g., phones)
- top plate consist of a thin film of **electret material** on which a metal payer is deposited
- thin film allows the flexibility and motion required in the microphone
- metal layers (top and bottom) are connected to a resistor
- output voltage across resistor used as output signal



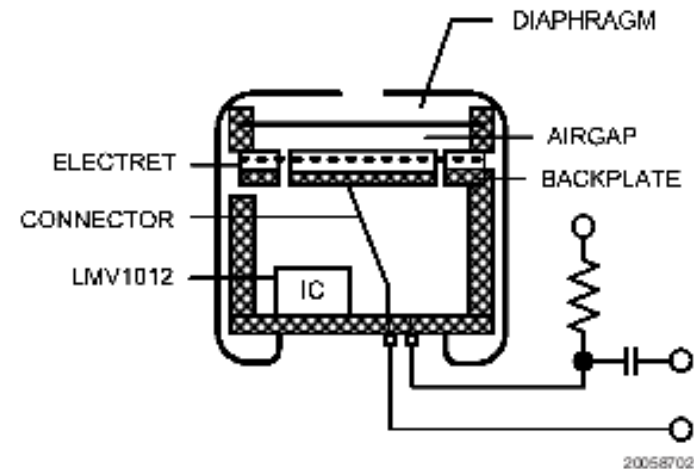
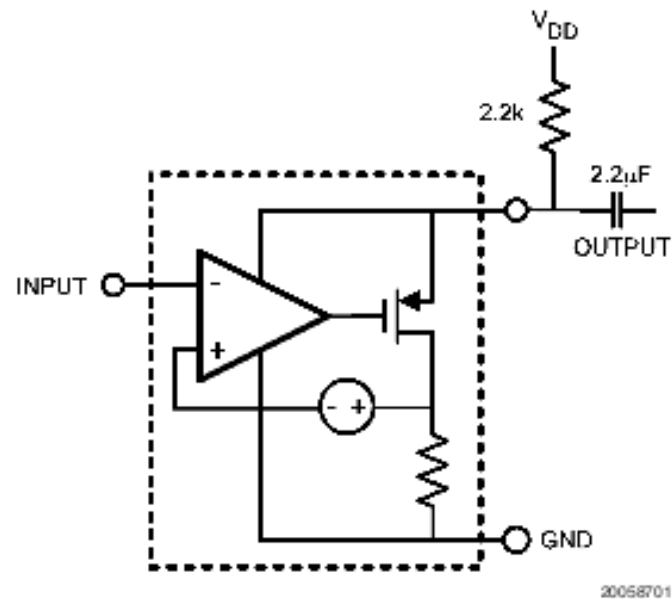
- electret has a constant charge density σ_1 on its surface
- charge density sets electric field E_1 in air gap
- acoustic wave on diaphragm reduces size of air gap from s_1 to $s_1 - \Delta s$
- when no circuit is connected, the difference in output voltage is equal to:

$$\Delta V = \frac{s \Delta s}{\epsilon_0 (s + \epsilon s_1)}$$

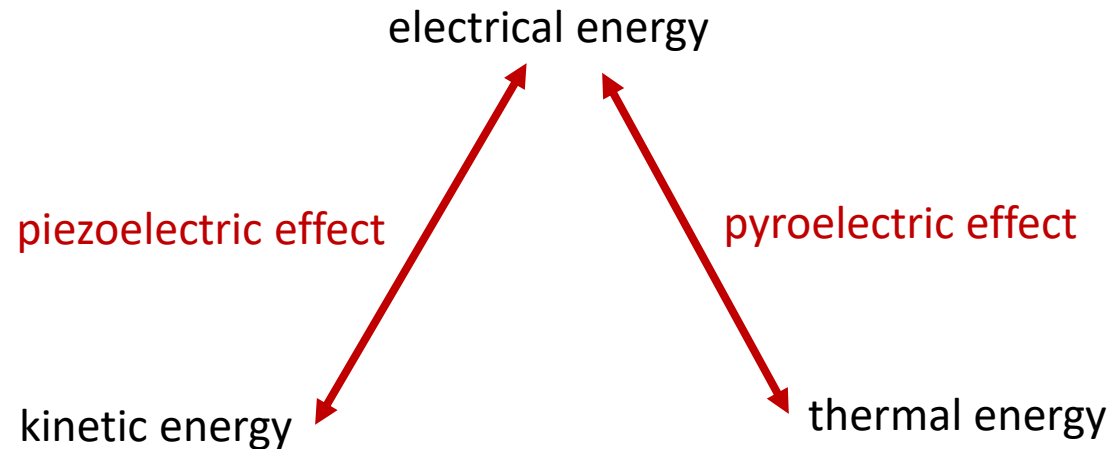
- ϵ – electret constant of material



- electret microphones are very popular
 - simple and inexpensive
 - do not require a voltage source
- their impedance is very high
 - circuit is needed to match high impedance to low impedance of processing circuit
 - FET pre-amplifier or amplifier can be used for this purpose



- crystalline materials generate electric charge when subjected to stress (**piezoelectric effect**)
- **pyroelectric effect** closely related to piezoelectric effect
- both effects are reversible

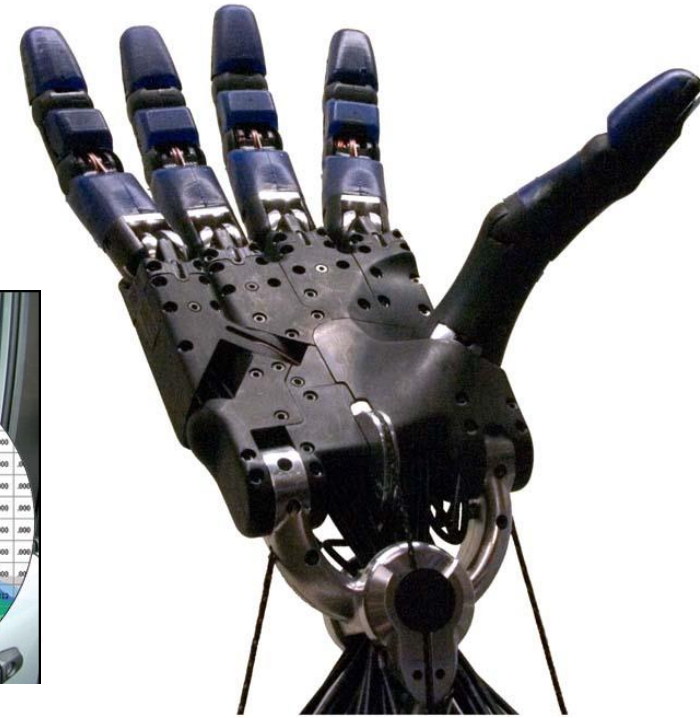
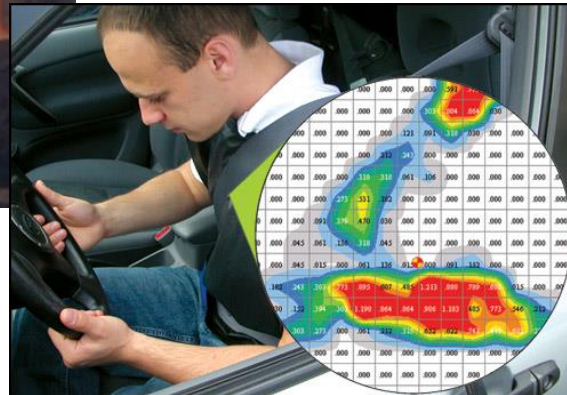


- piezoelectric effect exists in
 - natural crystals (e.g. quartz - SiO_2)
 - artificially polarized (poled) ceramics and polymers

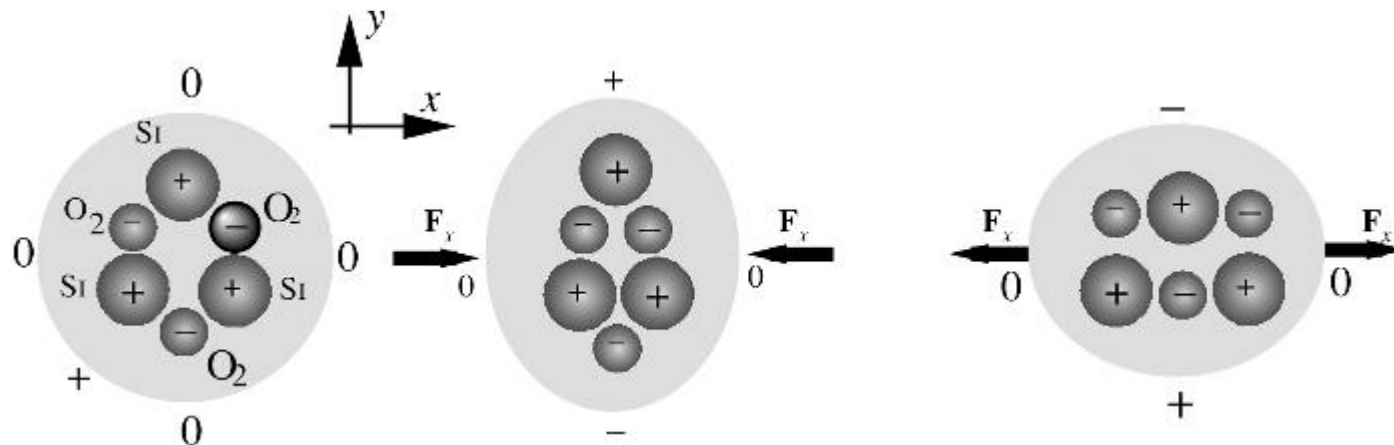


common rail injection system

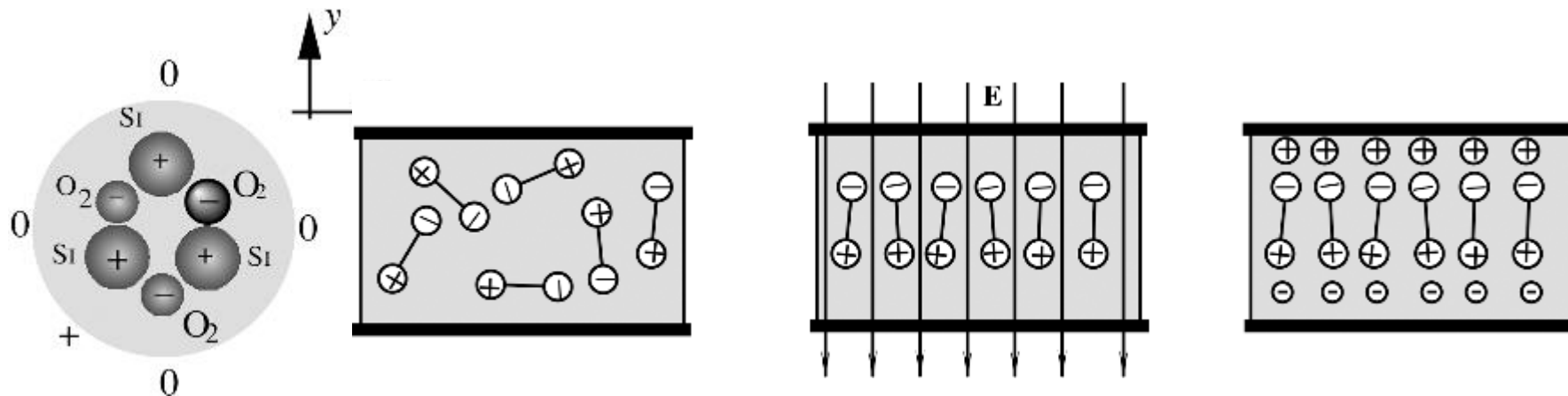




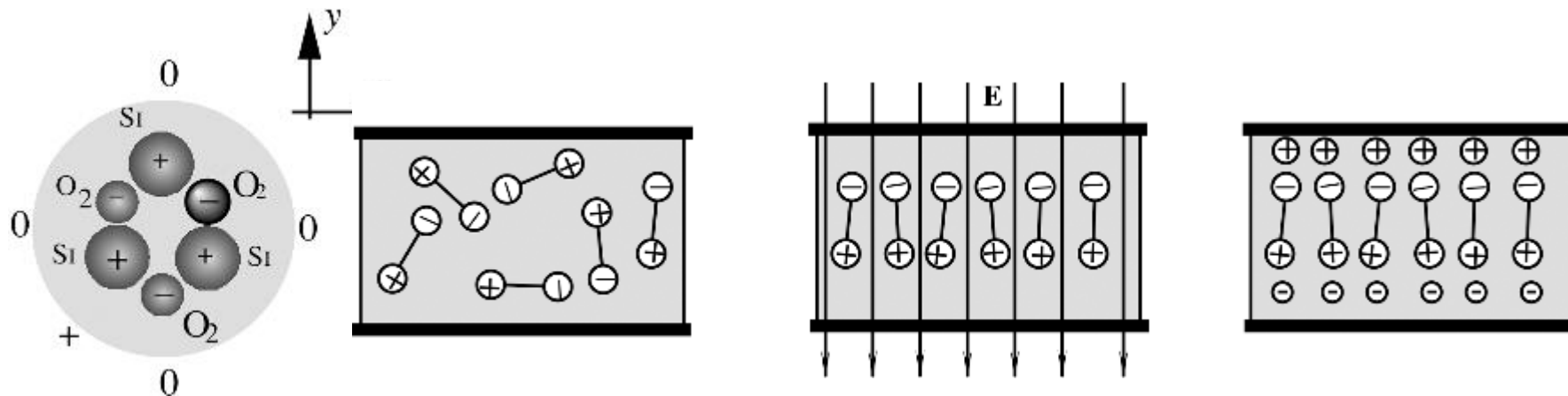
- quartz crystal model as helix
 - one silicon and two oxygen atoms alternating around helix
 - single cell (slice of helix) contains 3 Si atoms and 6 O atoms
 - Si has 4 positive charges, O has 2 negative charges
 - cell is electrically neutral
- compressing force in X direction leads to positive charge at top
- stretching force in Y direction leads to negative charge at top



- crystal cells can be considered **electrical dipoles**
 - cells may be naturally oriented along crystal axes (e.g. quartz)
 - dipoles may be oriented randomly, but dipoles can be “poled” into required orientation
- **thermal poling** is most commonly used technique for poling
 - warm up crystalline material till just below Curie temperature
 - apply strong electrical field to align dipoles
 - cool material down
 - remove electrical field
 - orientation of dipoles is “frozen” in direction of the electrical field



- thermal poling creates small charge on the plates
 - quickly dissipated by free charges from the surrounding atmosphere which are attracted to the plates
 - after a very short time, there will be no charge on the plates
- stress disturbs balanced state
 - charge will appear on the plates
- internal leakage will neutralize charge when stress is maintained
 - piezoelectric sensor is **sensitive to change**, not to steady-state



- charge on electrodes due to force F

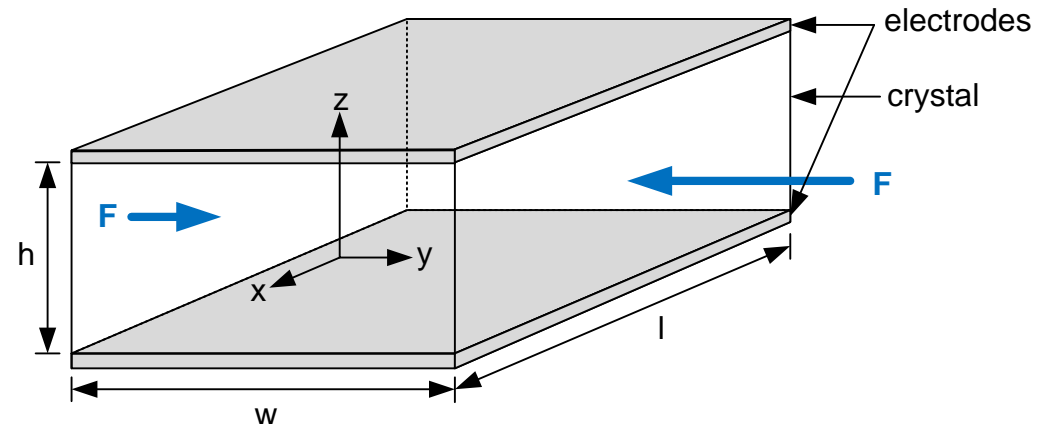
$$Q = d \frac{F}{l \cdot h} (w \cdot l)$$

- d – piezoelectric charge constant (pC/N)
- charge constant depends on position of force and electrodes
- capacitor relates charge and voltage

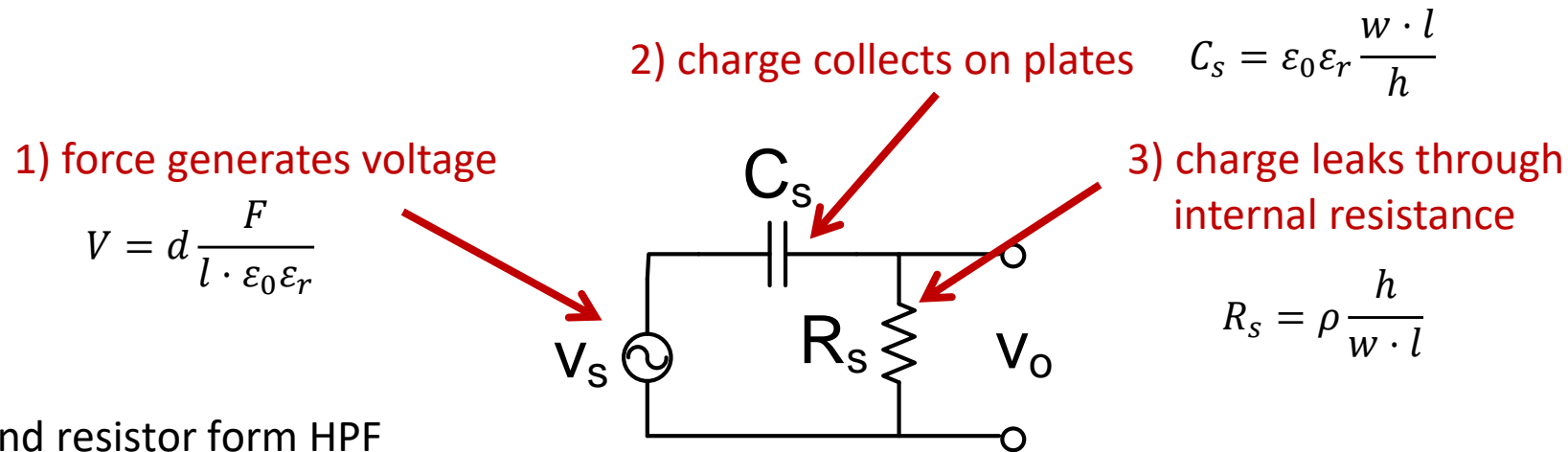
$$\left. \begin{array}{l} Q = CV \Rightarrow V = \frac{Q}{C} \\ C = \varepsilon_0 \varepsilon_r \frac{w \cdot l}{h} \end{array} \right\} \Rightarrow V = d \frac{F}{l \cdot h} (w \cdot l) \frac{h}{\varepsilon_0 \varepsilon_r \cdot w \cdot l} = d \frac{F}{l \cdot \varepsilon_0 \varepsilon_r}$$

- crystal has conductive properties
- resistive path between electrodes

$$R = \rho \frac{h}{w \cdot l}$$



- electrical equivalent circuit for sensor

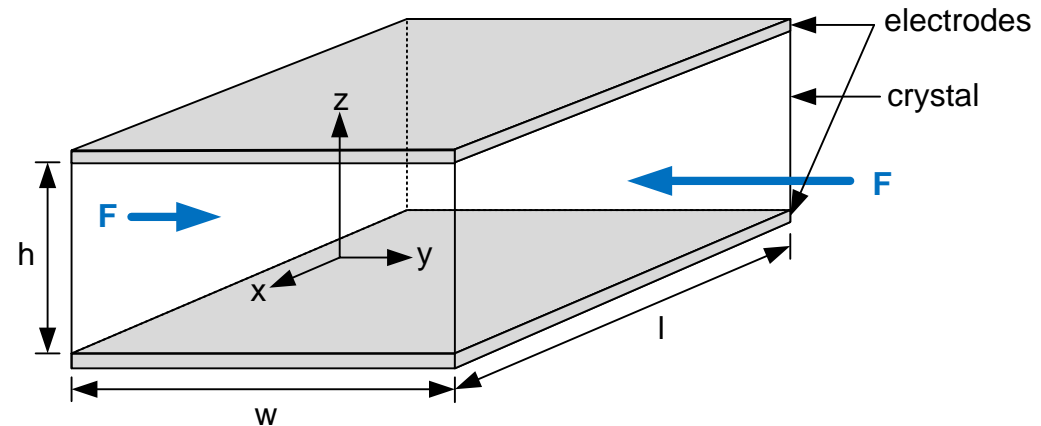


- capacitor and resistor form HPF

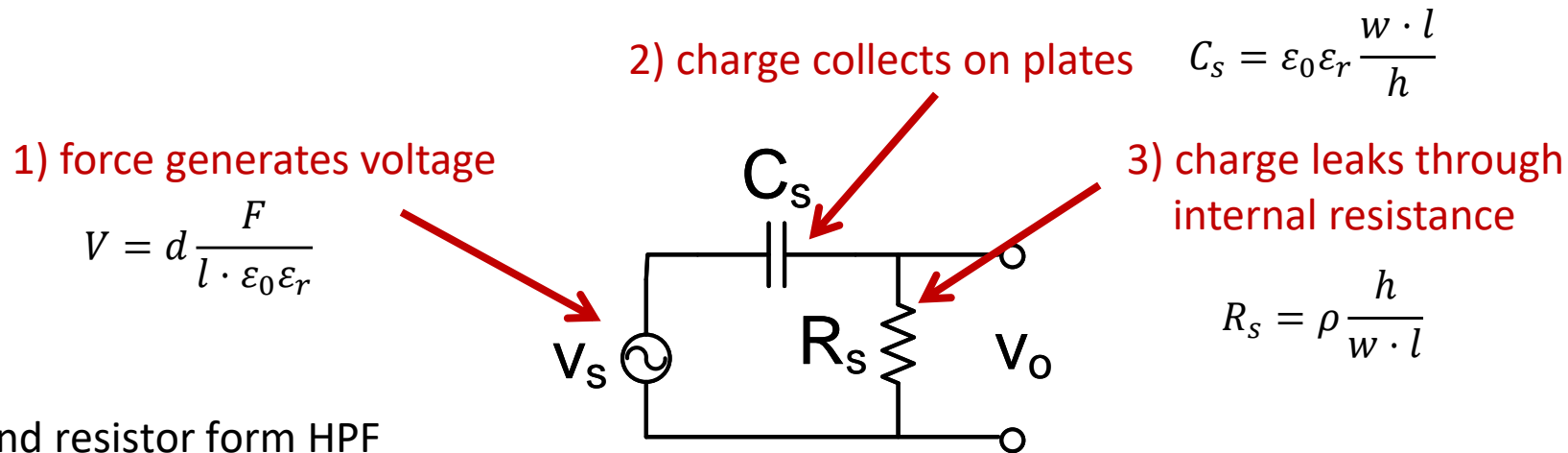
$$\left| \frac{v_o}{v_s} \right| = \left| \frac{j\omega R_s C_s}{1 + j\omega R_s C_s} \right| = \frac{\omega R_s C_s}{\sqrt{1 + (\omega R_s C_s)^2}}$$

- cut-off frequency

$$\omega_c = \frac{1}{R_s C_s}$$



- electrical equivalent circuit for sensor



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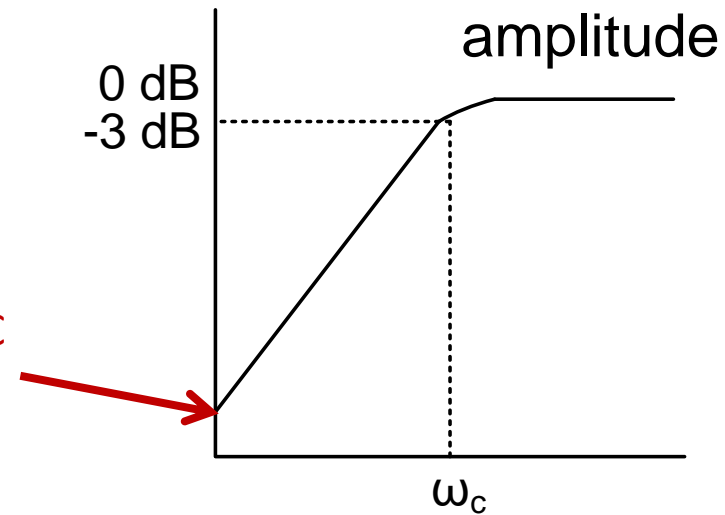
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- cut-off frequency

$$\omega_c = \frac{1}{R_s C_s}$$

- sensor only sensitive to changing force

sensor has no DC response

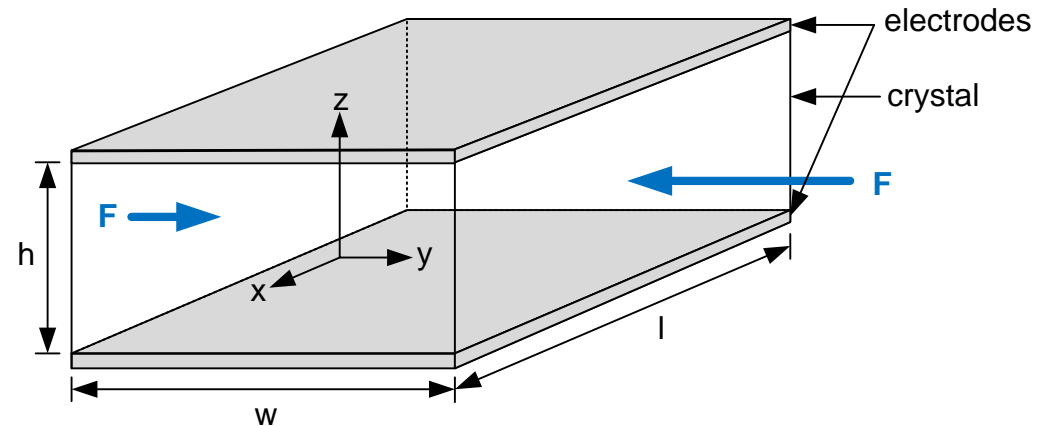


example – piezoelectric sensor

- $h = 52 \mu\text{m}$, $l = 10 \text{ cm}$, $w = 10 \text{ cm}$
- $d = 23 \text{ pC/N}$, $\epsilon_r = 12$, $\epsilon_0 = 8.85 \text{ pF/m}$, $\rho = 10 \text{ T}\Omega\cdot\text{m}$

what is the force generated voltage when a weight of 40 kg is applied to the sensor?

what is the minimal frequency of a dynamic compression for an allowed amplitude error of 5%?



example – piezoelectric sensor

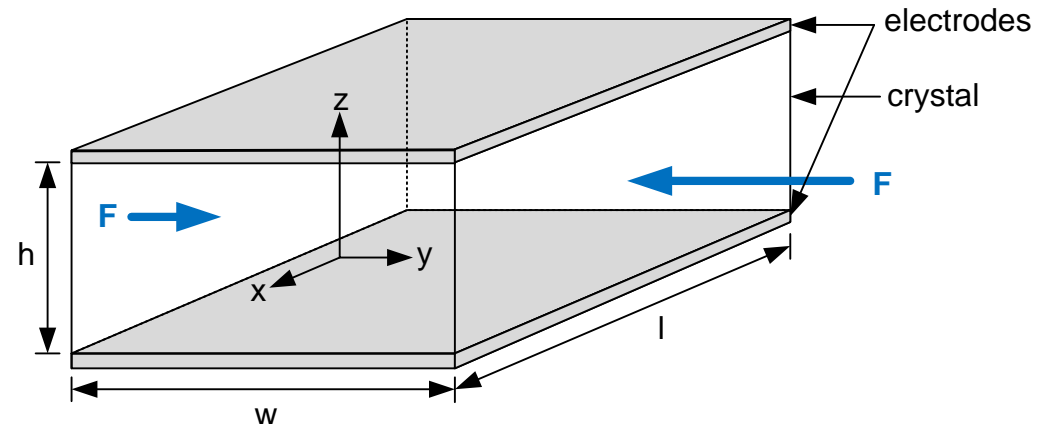
- $h = 52 \mu\text{m}$, $l = 10 \text{ cm}$, $w = 10 \text{ cm}$
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what is the force generated voltage when a weight of 40 kg is applied to the sensor?

$$V = d \frac{F}{l \cdot \epsilon_0 \epsilon_r} = (23 \text{ pC/N}) \frac{40 \cdot 9.8 \text{ N}}{(0.1 \text{ m}) \cdot (12 \cdot 8.85 \text{ pF/m})} = 849 \text{ V}$$

what is the minimal frequency of a dynamic compression for an allowed amplitude error of 5%?

constraint: $\left| \frac{v_o}{v_s} \right| = \frac{\omega R_s C_s}{\sqrt{1 + (\omega R_s C_s)^2}} = \frac{1}{\sqrt{1 + \left(\frac{\omega_c}{\omega} \right)^2}} > 0.95$



example – piezoelectric sensor

- $h = 52 \mu\text{m}$, $l = 10 \text{ cm}$, $w = 10 \text{ cm}$
- $d = 23 \text{ pC/N}$, $\epsilon_r = 12$, $\epsilon_0 = 8.85 \text{ pF/m}$, $\rho = 10 \text{ T}\Omega\cdot\text{m}$

what is the minimal frequency of a dynamic compression for an allowed amplitude error of 5%?

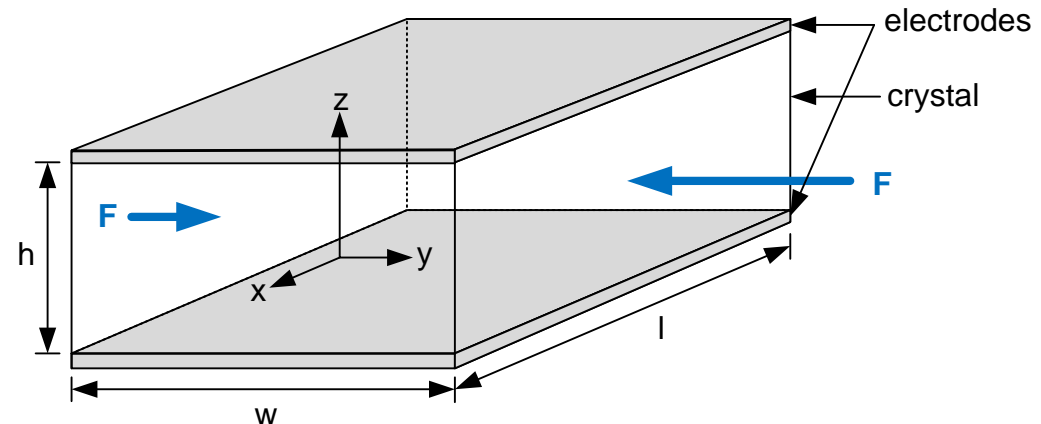
$$R_s = \rho \frac{h}{w \cdot l} = (10 \cdot 10^{12} \Omega\text{m}) \frac{52 \mu\text{m}}{0.1\text{m} \cdot 0.1\text{m}} = 52 \text{ G}\Omega$$

$$C_s = \epsilon_0 \epsilon_r \frac{w \cdot l}{h} = 12 \cdot 8.85 \text{ pF/m} \cdot \frac{0.1\text{m} \cdot 0.1\text{m}}{52 \mu\text{m}} = 20.4 \text{ nF}$$

$$\left. \vphantom{\frac{1}{R_s C_s}} \right\} \Rightarrow \omega_c = \frac{1}{R_s C_s} = 1 \cdot 10^{-3} \text{ rad/s}$$

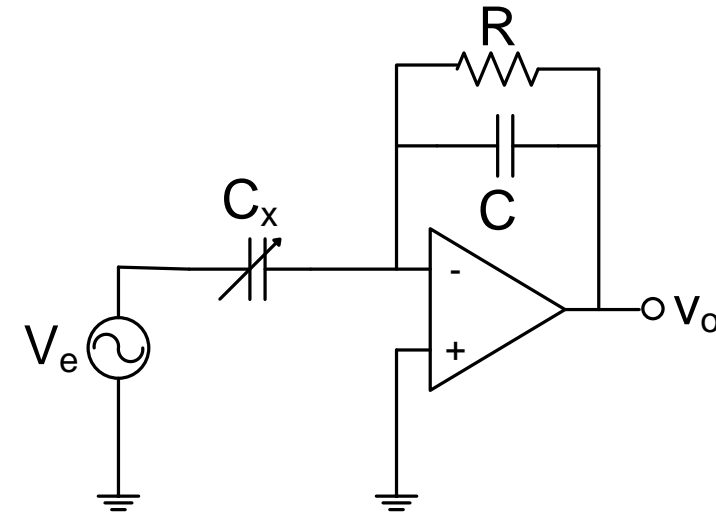
constraint: $\frac{1}{\sqrt{1 + \left(\frac{\omega_c}{\omega}\right)^2}} > 0.95$

$$\Rightarrow \omega > 0.003 \text{ rad/s} \Leftrightarrow f > 0.02 \text{ Hz}$$

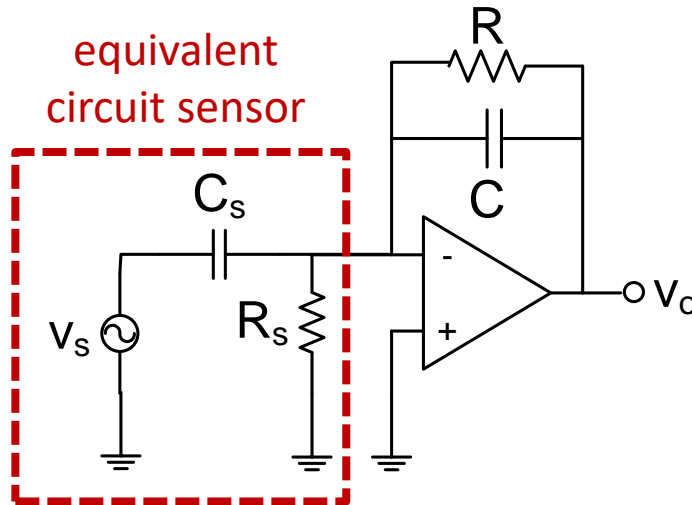


- charge amplifier circuit
 - R provides bias current path
 - output voltage

$$v_o = -\frac{C_x}{C} v_e$$



- charge amplifier can be used to get charge of piezoelectric sensor



$$\left. \begin{aligned} v_o &= -\frac{C_s}{C} v_s \\ v_s &= \frac{Q_s}{C_s} \end{aligned} \right\} \Rightarrow v_o = -\frac{C_s}{C} \frac{Q_s}{C_s} = -\frac{Q_s}{C}$$

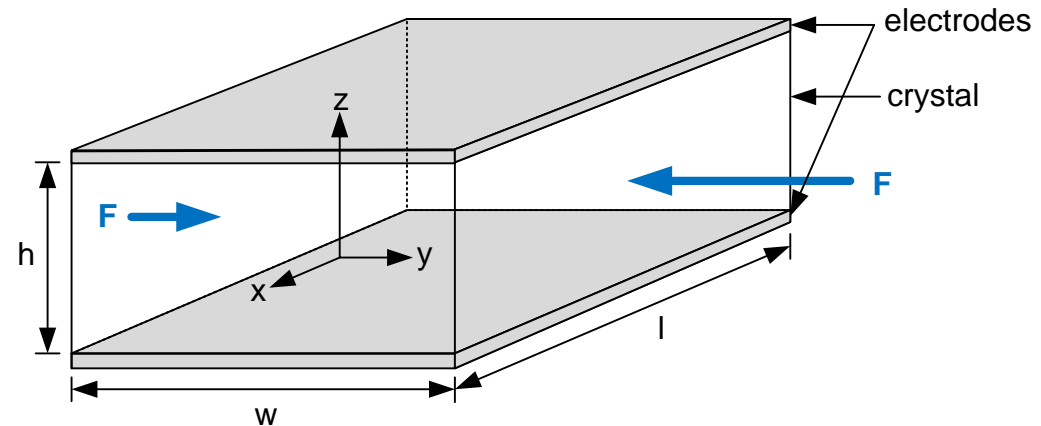
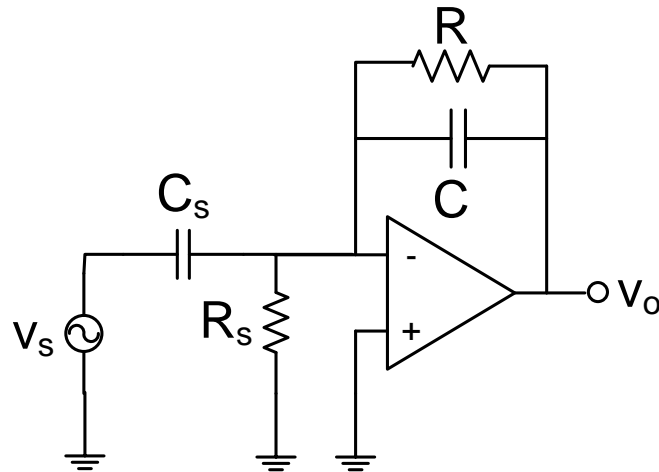
$$\Leftrightarrow v_o = -\frac{Q_s}{C} \quad \left. \begin{aligned} Q_s &= d \frac{F}{l \cdot h} (w \cdot l) \end{aligned} \right\} \Rightarrow v_o = -d \frac{F}{l \cdot h} (w \cdot l) \frac{1}{C}$$

example – piezoelectric sensor

- $h = 52 \mu\text{m}$, $l = 10 \text{ cm}$, $w = 10 \text{ cm}$
- $d = 23 \text{ pC/N}$, $\epsilon_r = 12$, $\epsilon_0 = 8.85 \text{ pF/m}$, $\rho = 10 \text{ T}\Omega\cdot\text{m}$
- $C_s = 20.4 \text{ nF}$, $R_s = 52 \text{ G}\Omega$

what value should the capacitor C have to get an output sensitivity of -10 mV/Pa?

$$v_o = -d \frac{F}{l \cdot h} (w \cdot l) \frac{1}{C} \Rightarrow -10 \text{ mV} = -23 \text{ pC/N} (1 \text{ N/m}^2) (0.1 \text{ m} \cdot 0.1 \text{ m}) \frac{1}{C} \Rightarrow C = 23 \text{ pF}$$



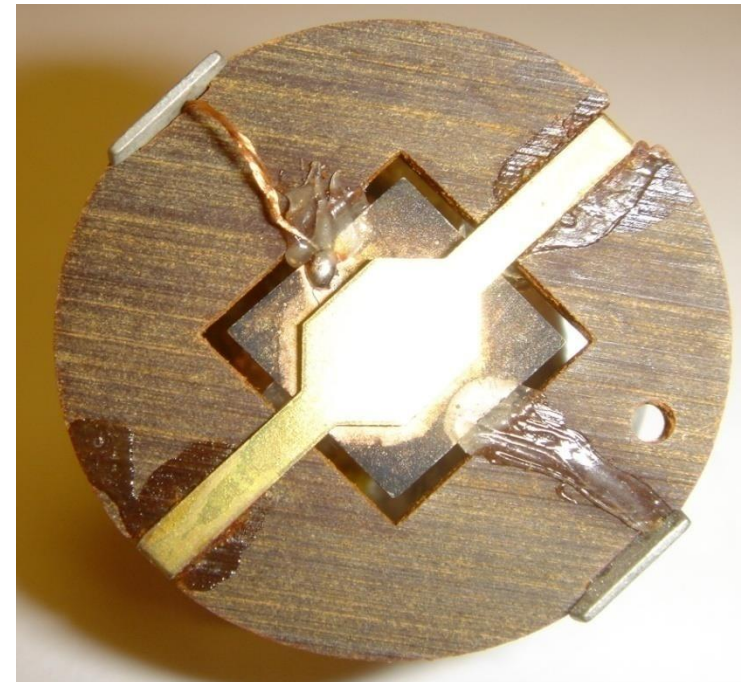
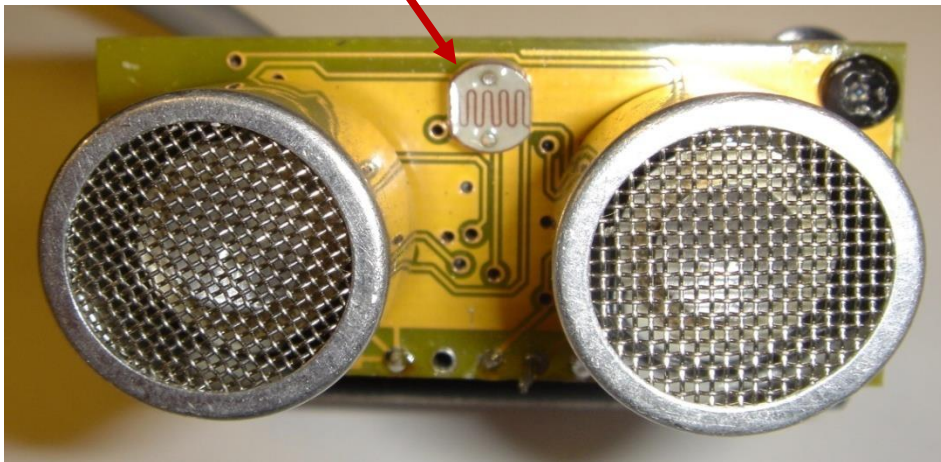
- piezoelectric speakers (actuator)
 - used in many electronics devices (e.g., computer, watch)
 - piezoelectric speakers are resistant to overloads
 - provide direct conversion of electrical to mechanical energy
 - other speaker use magnetic field to move cone
 - their frequency response is inferior to that of other technologies
 - generally used in single frequency (beeper) applications
- piezoelectric speaker can also be used to convert mechanical energy (sound) to electrical energy
- **actuator** (speaker) can be used as **sensor** (microphone)



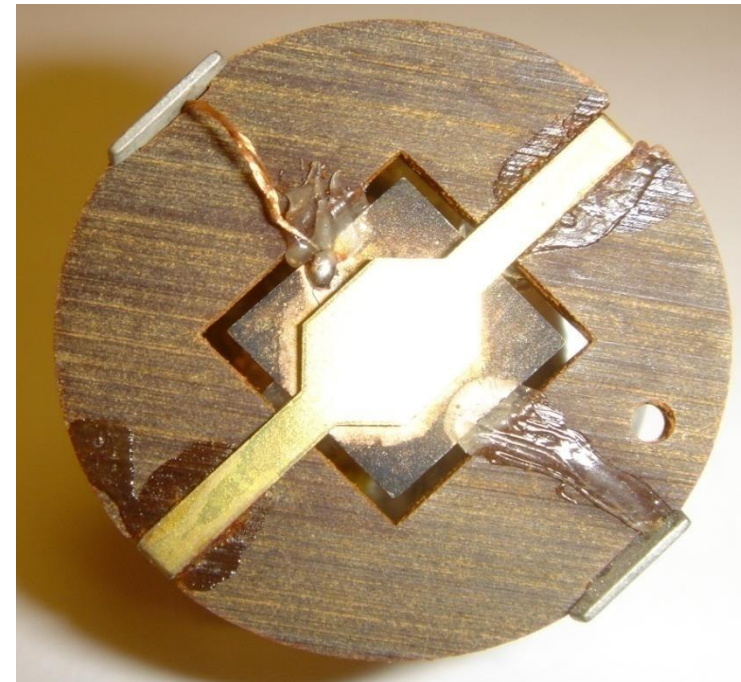
- ultrasonic range starts where audible range ends
- basic principles of ultrasound sensors identical to acoustic sensors
- therefore ultrasound sensors for the near ultrasound range are quite similar to acoustic sensors
- construction, materials used, and frequency range are different
- example: 40kHz UT transmitter and receiver
 - transmitter and receiver have essentially the same construction
 - both use an identical piezoelectric disk
 - only difference is in the construction of the cone



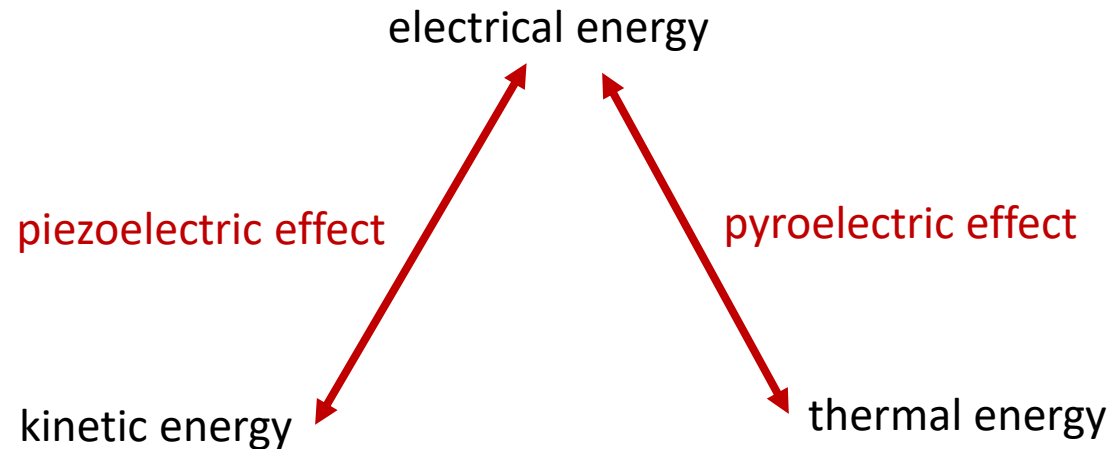
- example: 40kHz ultrasonic sensor
 - sensor contains piezoelectric element (square in center)
 - one electrode connected to top of piezoelectric element
 - other wire is connected underneath brass element which supports sensor
 - can be used in pair to measure distance (range finding)
 - notice the thermal sensor (speed of sound is highly temperature dependent)



- example: 40kHz ultrasonic actuator
 - actuator contains piezoelectric element (square in center)
 - piezoelectric materials can oscillate at a fixed, sharply defined frequency (resonant frequency)

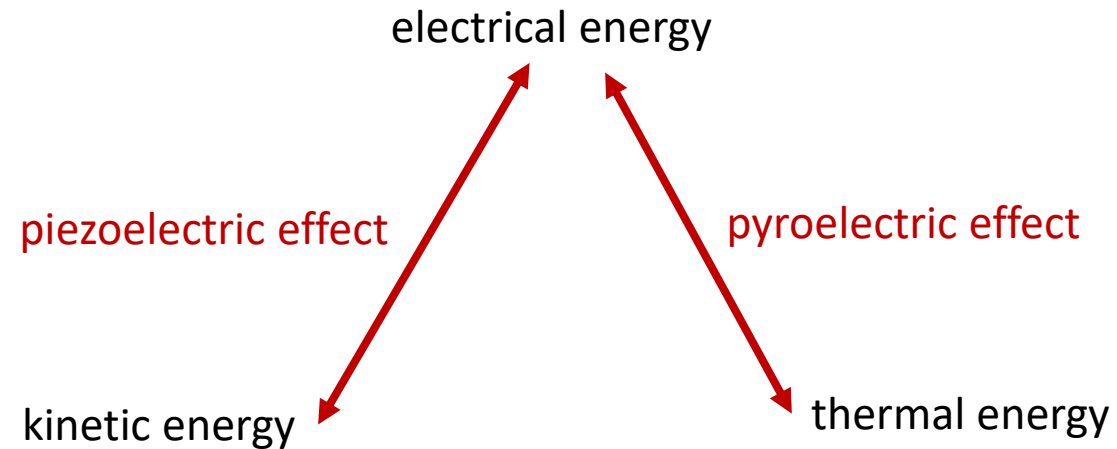


- crystalline materials generate electric charge when subjected to stress (**piezoelectric effect**)
- **pyroelectric effect** closely related to piezoelectric effect
- both effects are reversible

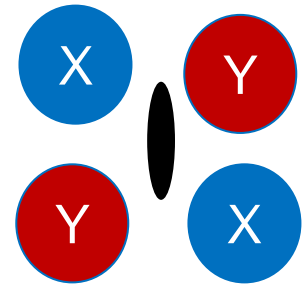


- piezoelectric effect exists in
 - natural crystals (e.g. quartz - SiO_2)
 - artificially polarized (poled) ceramics and polymers

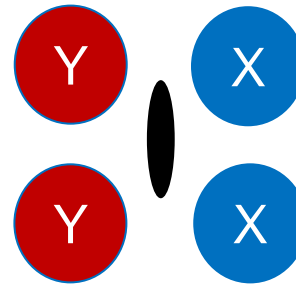
- **pyroelectricity** is the ability of certain materials to generate an electrical charge in response to heat flow
- pyroelectric effect is closely related to piezoelectric effect



- material has center of symmetry when each atom in an imaginary unit cell has an exact twin opposite to it on a line through an imaginary center point

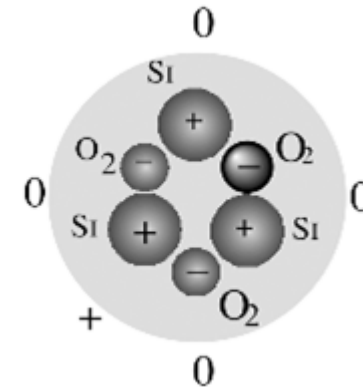


symmetric cell

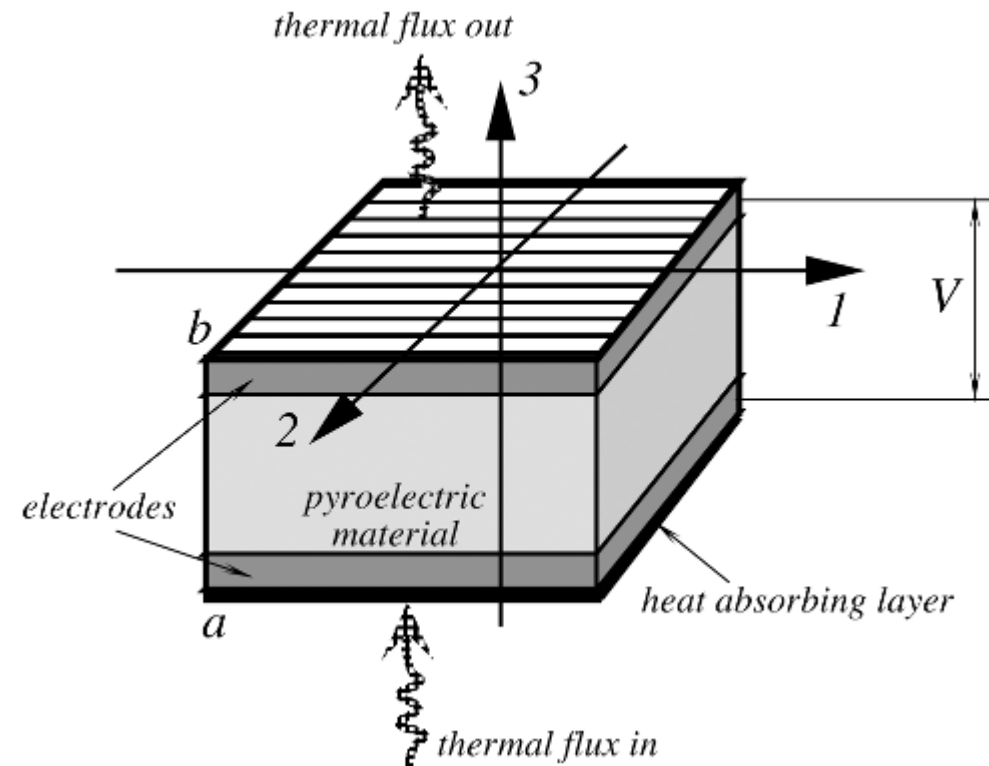


non-symmetric cell

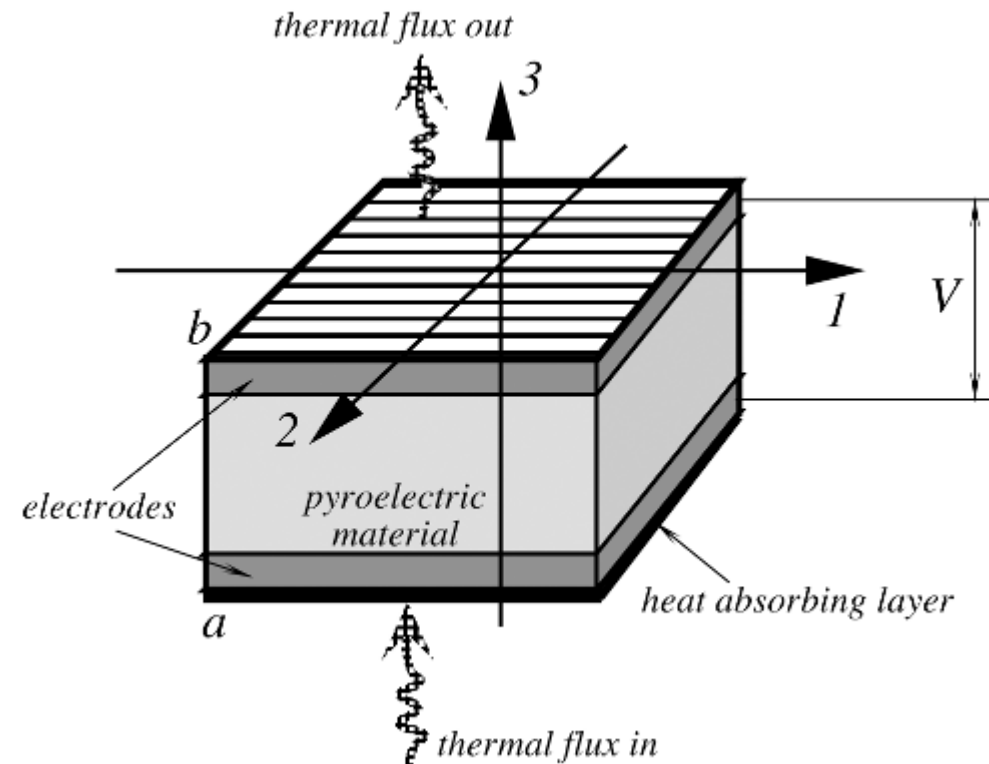
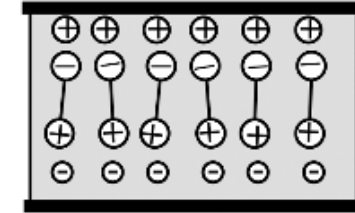
- force on symmetric cell will never cause a dipole to appear
- piezoelectric materials have no center of symmetry
 - some piezoelectric materials show temperature dependent polarization
 - these materials are called pyroelectric



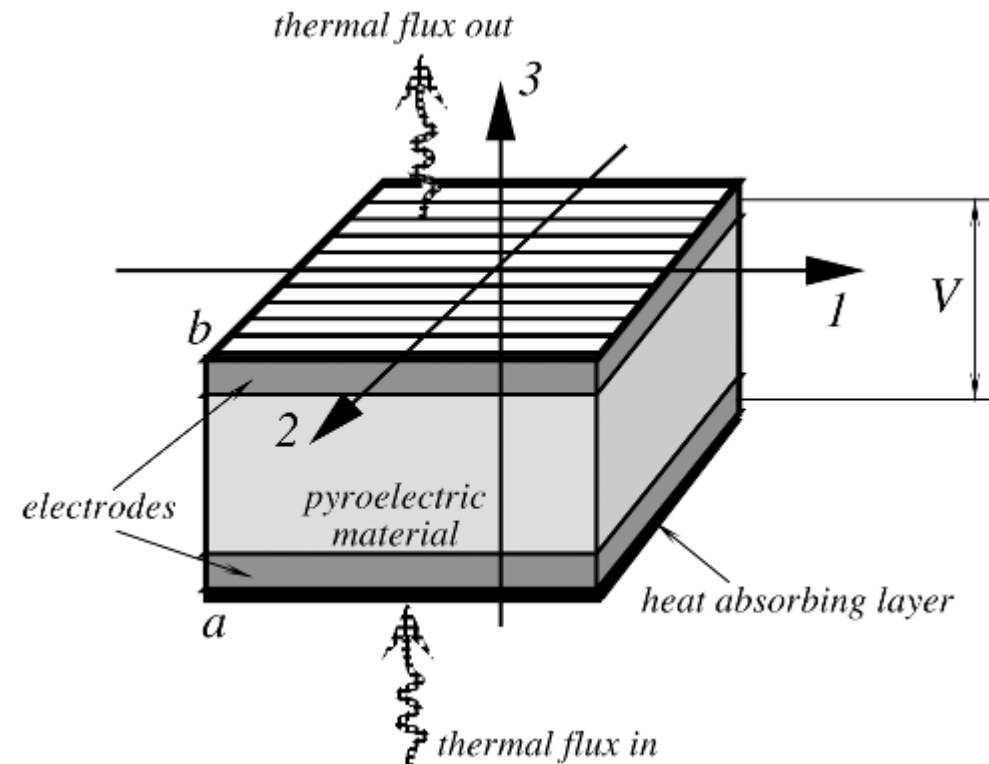
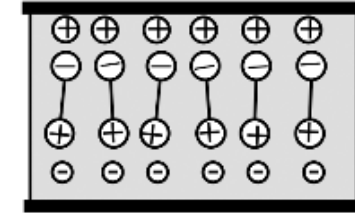
- pyroelectric sensor
 - same construction as piezoelectric sensor
 - passive (**self-generating**) sensor
 - responds to change in temperature (**dynamic**)
 - no response to temperature (**steady-state**)



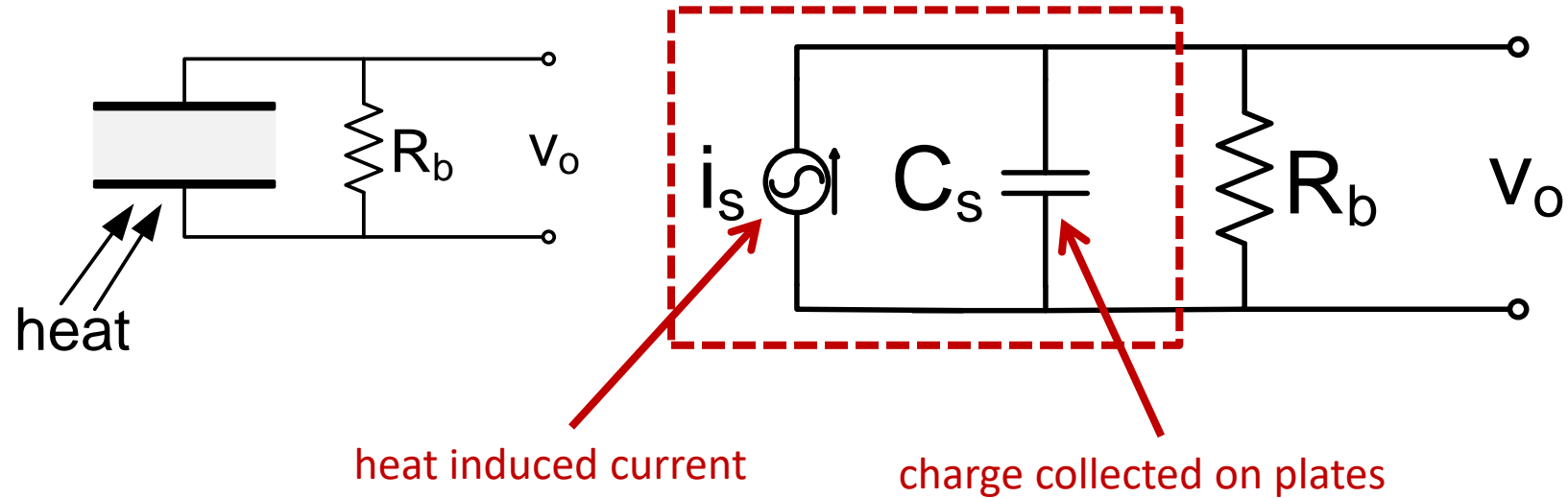
- pyroelectricity is the ability of certain materials to generate an electrical charge in response to heat flow
- pyroelectricity caused by two mechanisms
 - mechanism 1: temperature changes cause
 - shortening or elongation of individual dipoles
 - randomness of dipole orientation changes due to thermal agitation



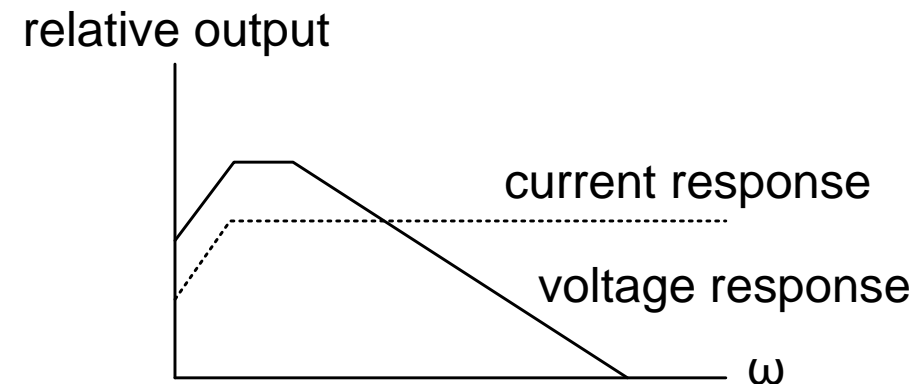
- pyroelectricity is the ability of certain materials to generate an electrical charge in response to heat flow
- pyroelectricity caused by two mechanisms
 - mechanism 2: strain due to thermal expansion creates piezoelectric effect
 - thermal radiation absorbed by sensor as heat
 - heat propagates to pyroelectric material
 - creates thermally induced stress



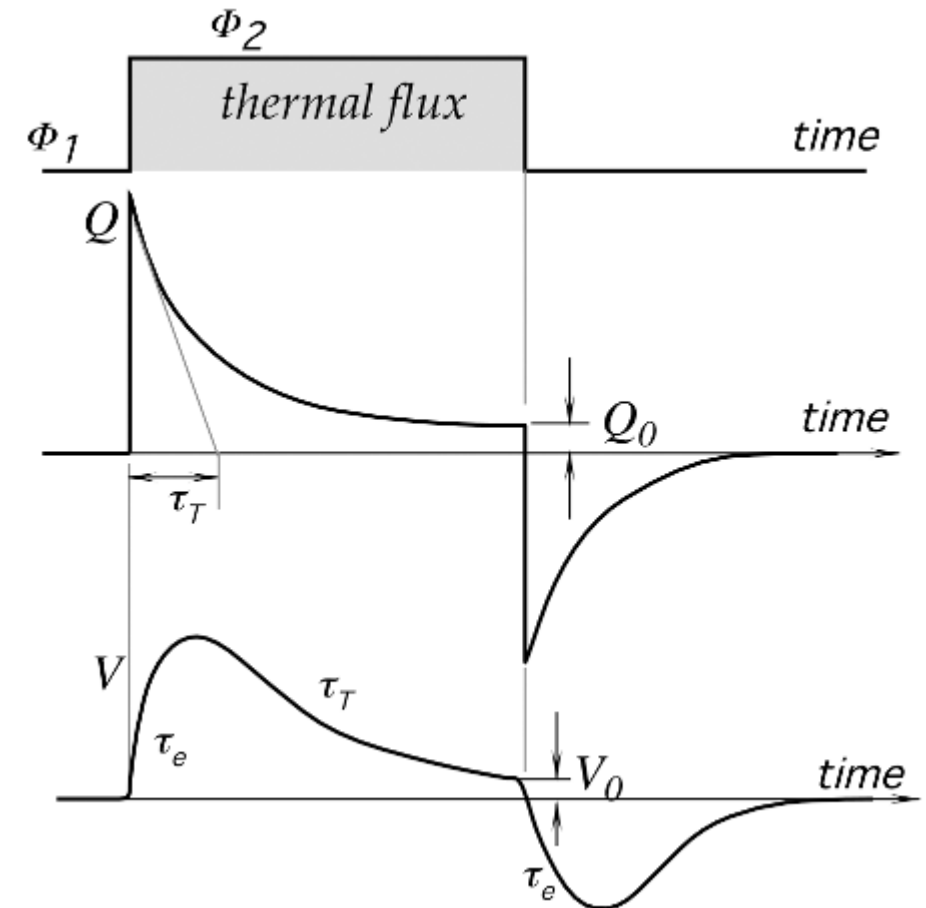
- pyroelectric sensor connected to a resistor R_b



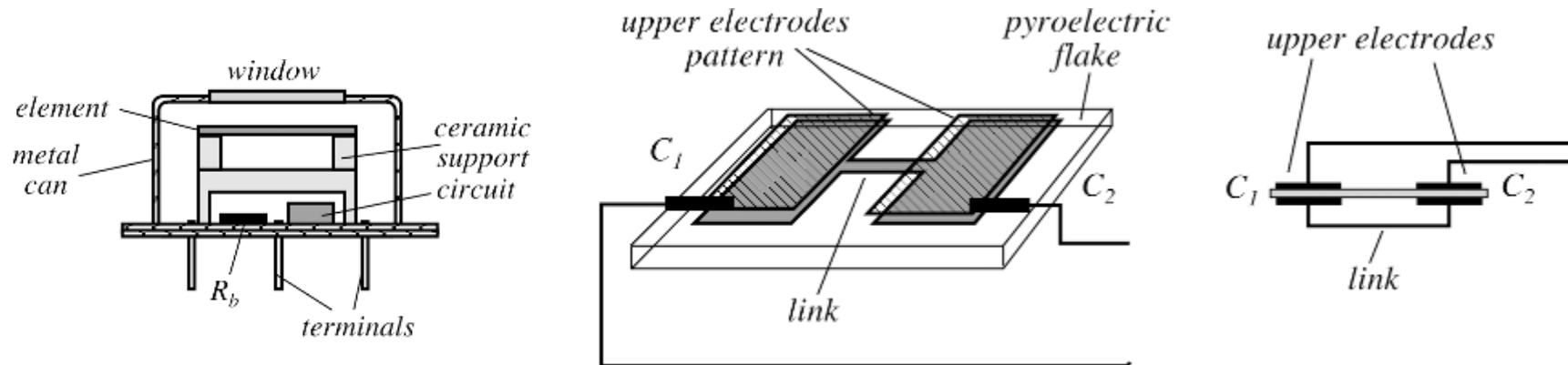
- ignore internal leakage since $R_b \ll R_s$
- capacitor discharged through R_b
- measure output of sensor as
 - current through R_b (flow of charge)
 - voltage across R_b (charge build-up)



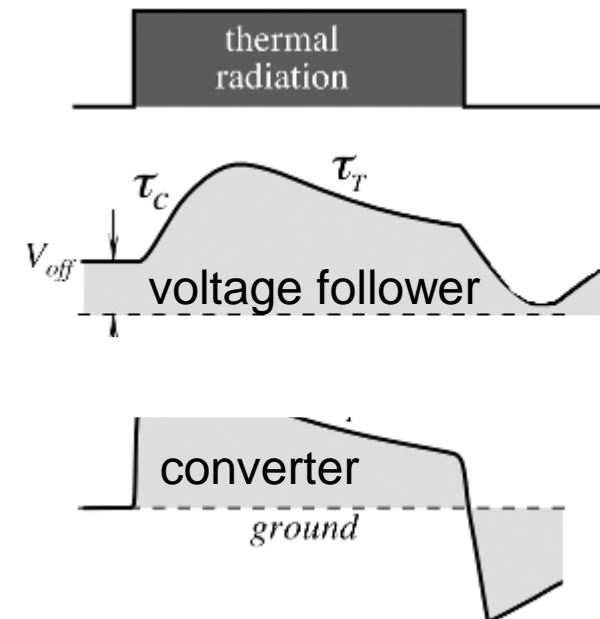
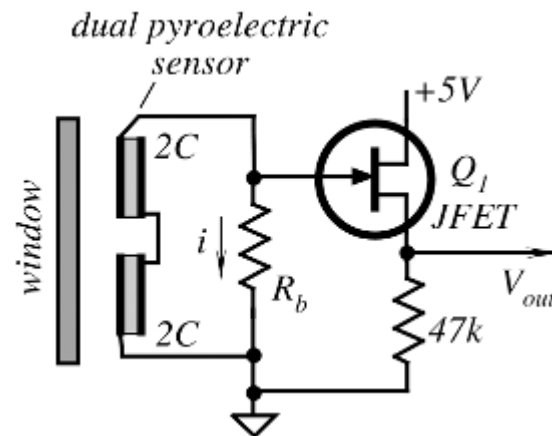
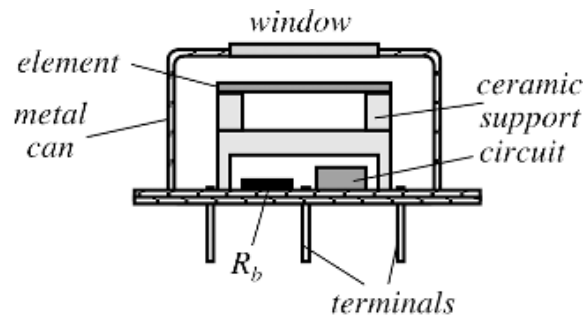
- pyroelectric sensor exposed to step function of heat
- electric charge (Q) reaches peak value instantaneously
- thermal induced polarization occurs initially only at outermost layers
 - outer layers reach maximal temperature instantaneously
 - creates highest thermal gradient and maximal polarization
- electric charge decays as heat propagates through material
- part of heat lost to surrounding environment
 - result in voltage V_0
 - use sensor to measure (constant) heat flow



- pyroelectric sensors belong to class of **passive infrared sensors**
- thermal energy reaches sensor element through window
- often two sensor elements for compensation of mechanical stress



- solution 1: **voltage follower**
 - voltage across bias resistor R_b is followed by voltage V_{out}
 - response time depends on electrical time constant ($\tau_e = C \cdot R_b$)
 - typically 2 seconds
 - upper cut-off frequency around 0.08Hz
 - only suitable for slow moving objects (e.g. people)
 - offset voltage at output due output resistor



- solution 2: **current-to-voltage converter**
 - output voltage follows shape of current
 - faster response
 - insensitive to sensor capacitance
 - feedback forces output voltage of sensor to zero

