

Formulae sheet - Sensor, Computing, Actuating (5AIB0)

A copy of this formulae sheet will be distributed as part of the interim and final exam of “Sensing, Computing, Actuating” (5AIB0). The sheet may be used as reference material during these exams. Note: some questions on the exam may require you to know formulas that are not listed on this sheet.

Characteristic temperature of material: $B_{T_1/T_2} = \frac{\ln\left(\frac{R_2}{R_1}\right)}{\frac{1}{T_2} - \frac{1}{T_1}}$

Resistance: $R = \frac{m}{ne^2\tau} \frac{l}{A} = \rho \frac{l}{A}$

Strain: $\epsilon = \frac{dl}{l}$

Stress: $\sigma = \frac{F}{A} = E \frac{dl}{l}$

Poisson's ratio: $\nu = -\frac{dt/t}{dl/l}$

Change in specific resistance due to volume change (for metals): $\frac{d\rho}{\rho} = C \frac{dV}{V}$

Change in resistance due to strain: $\frac{dR}{R} = G\epsilon$

Capacitance of flat plate capacitor: $C = \frac{q}{V} = \epsilon_0\epsilon_r \frac{A}{d}$

Capacitance of cylindrical capacitor: $C = \frac{q}{V} = \epsilon_0\epsilon_r \frac{2\pi \cdot l}{\ln(b/a)}$

Energy stored in capacitor: $E = \frac{C \cdot V^2}{2}$

Reluctance: $\mathfrak{R} = \frac{1}{\mu\mu_0} \frac{l}{A}$

Inductance: $L = \frac{N \cdot \Phi}{i} = \frac{N^2}{\mathfrak{R}}$

Flux: $\Phi = \mathbf{B} \times \mathbf{S}$

Magneto-motive force: $F_m = \Phi \cdot \mathfrak{R} = N \cdot i$

Amplitude response of Butterworth LPF: $|H(f)| = \frac{1}{\sqrt{1 + \left(\frac{f}{f_n}\right)^{2n}}}$

Sideways force on electron moving through magnetic field: $\mathbf{F} = q \cdot \mathbf{v} \times \mathbf{B}$

Transverse Hall potential: $V_H = \frac{1}{N \cdot c \cdot q} \frac{i \cdot B}{d} \sin(\alpha)$

Radius of warping of bimetal sensor: $r \approx \frac{2j}{3(\alpha_x - \alpha_y)(T_2 - T_1)}$

Displacement of bimetal sensor: $\Delta = r(1 - \cos\left(\frac{180L}{\pi r}\right))$

Flow velocity and temperature difference: $v = \frac{K}{\rho} \left(\frac{e^2}{R_S} \frac{1}{T_s - T_0} \right)^{1.87}$

Voltage across P-N junction (quality factor 1): $V = \frac{kT}{q} \ln\left(\frac{I}{I_0}\right)$

Saturation current through PN-junction (quality factor 1): $I_0 = BT^3 e^{-E_g/kT}$

Thomson effect: $Q = I^2 \cdot R - I \cdot \sigma \frac{dT}{dx}$

Peltier coefficient: $\pi_{AB}(T) = T \cdot (\alpha_A - \alpha_B) = -\pi_{BA}(T)$